

# Asymmetric Information

- hidden information problem or  
"pre contractual opportunism"
- hidden action problem or  
"post contractual opportunism",  
"moral hazard"

Hidden information

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"The market for Lemons"

MARKET FREQUENCY

A SECON-HAND CAR MARKET WITH ASYMMETRIC INFORMATION BETWEEN BUYERS AND SELLERS

100 buyers  
100 sellers

cars

H HIGH  
QUALITY

$$\pi_H = 1/2$$

L LOW  
QUALITY

$$\pi_L = 1/2$$

$$p^S = 2000$$

$$p_L^S = 1000$$

seller's reservation price of H  
" " " " L

buyers' reservation prices:

$$p_H^d = 2400$$

$$p_L^d = 1200$$

$$E(p^d) = \pi_H \cdot p_H^d + \pi_L \cdot p_L^d = 1800$$

$$E(p^d) < p_H^s$$

ADVERSE  
SELECTION

ADVERSE SELECTION IS THE PROCESS BY WHICH THE EXCESSIVE FREQUENCY OF LOW-QUALITY GOODS MAKES HIGH-QUALITY GOODS LEAVE THE MARKET  
THIS CAUSES AN ENDOGENOUS CHANGE IN FREQUENCY OF H AND L TYPES:

$$\Rightarrow \pi_H = 0 \quad \pi_L = 1$$
$$\Rightarrow E(p^d) = p_L^d$$

insurance

H high risk profile

$\pi_H$  risk of  
bad  
event

L low risk profile

$\pi_L$

$f_H$  frequency of H agents

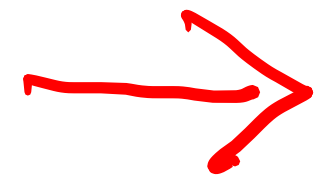
$$\pi_L < \pi_H$$

$f_L$  ~ ~ ~ L ~

average probability of 'bad event' =  $\bar{\pi} = f_H \pi_H + f_L \pi_L$

suppose premium  $\delta = \bar{\pi}$

$$\pi_L < \bar{\pi}$$



THE LOW-RISK AGENT CHOOSES  $K < D$  even if risk averse

$$\pi_H > \bar{\pi}$$



THE HIGH-RISK AGENT CHOOSES  $K = D$  even if risk neutral

The insurance company has a portfolio of contracts such that frequency of H contracts of the portfolio is  $\frac{K_H}{K_H + K_L} > p_H$

THE PROBABILITY THAT A BAD EVENT OCCURS IN THE POPULATION OF AGENTS BUYING INSURANCE IS HIGHER THAN THE PROBABILITY OF A BAD EVENT IN THE ENTIRE POPULATION OF AGENTS

an insurance company fixing  
 $\gamma = \bar{\pi}$  goes bankrupt

THE INSURANCE COMPANY IS AWARE OF THE PROBLEM AND WILL FIX A PREMIUM CORRESPONDING TO THE HIGH-RISK PROFILE:

$\gamma = \pi_H \rightarrow$  adverse  
selection  
the low-risk agents  $L$  leave  
the market

OR BUY ONLY VERY SMALL AMOUNTS OF INSURANCE



as IN THE CASE OF CAR INSURANCE, THE GOVERNMENT MAY DECIDE TO ADOPT A POLICY OF

mandatory insurance

BEING FORCED BY LAW,

H and

agents buy insurance

$K = 0$

$\Rightarrow$

$\theta = \pi$

NOW THE INSURANCE COMPANY CAN FIX A PREMIUM CORRESPONDING TO THE AVERAGE PROBABILITY OF A BAD EVENT IN THE ENTIRE POPULATION, WITHOUT GOING BANKRUPT

one solution to  
adverse selection is:

L low productivity  
type  
H high prod.  
type  
Labour market

$$a_H \quad y_H = a_H L_H$$

$$a_L \quad y_L = a_L L_L$$

$$a_H > a_L$$

$$S_H > S_L$$

reservation wages

$$W_H^R = W_L^R = W^R$$

if

$$W_H^A > W^R$$
$$W_L^A > W^R$$

Fixed  
Labor  
supply

FOR SIMPLICITY, WE ASSUME HERE THAT H AND L HAVE THE SAME  
RESERVATION WAGE. THEY DECIDE TO WORK IF THEY ARE OFFERED A WAGE  
NOT LOWER THAN THE RESERVATION WAGE (PARTICIPATION CONSTRAINT)



FREQUENCY OF TYPE H

$$\pi_H = \frac{S_H}{S_L + S_H}$$

FREQUENCY OF TYPE L

$$\pi_L = \frac{S_L}{S_L + S_H}$$

with no asymmetric information

ON THE ASSUMPTION THAT THE FIRM IS A MONOPSONIST ON THE

LABOUR MARKET, IT WILL OFFER THE LOWEST POSSIBLE WAGE MEETING THE

WORKER'S PARTICIPATION CONSTRAINT

$$W_L = W^R = W_H$$

worker's participation constraint

$$W_L \geq W_L^R = W^R$$

$$W_H \geq W_H^R = W^R$$

WITH NO ASYMMETRIC INFORMATION H AND L AGENTS ARE INDUCED TO SIGN DIFFERENT CONTRACTS:

IF AN AGENT OF TYPE

H

PRODUCES IN 1 HOUR OUTPUT

$a_H$

(OR HIGHER) GETS A WAGE =

$$W_H = W^R$$

$W_H = 0$  OTHERWISE

IF AN AGENT OF TYPE

L

PRODUCES IN 1 HOUR OUTPUT

$a_L$

(OR HIGHER), GETS WAGE =

$$W_L = W^R$$

$W_L = 0$  OTHERWISE.

THIS TYPE OF CONTRACT IS

Take it or leave it

- (1) SINCE THE WAGE IS NOT LOWER THAN THE RESERVATION WAGE, THE H AND L WORKER IS WILLING TO SIGN THE CONTRACT. THUS THE CONTRACT MEETS THE PARTICIPATION CONSTRAINT.
- (2) THE WAGE THE WORKER GETS BY EXERTING HER FULL PRODUCTIVITY POTENTIAL IS HIGHER THAN THE WAGE SHE GETS OTHERWISE. THEREFORE IT IS IN THE INTEREST OF THE L WORKER TO PRODUCE  $a_L$  AND IT IS IN THE INTEREST OF THE H WORKER TO PRODUCE  $a_H$ . THE CONTRACT MEETS THE "INCENTIVE COMPATIBILITY CONSTRAINT".
- (3) WITH ASYMMETRIC INFORMATION THIS CONTRACT IS NO LONGER AVAILABLE BECAUSE A HIGH PRODUCTIVITY WORKER HAS NO INCENTIVE TO SIGN: BY SO DOING HE WOULD GET THE SAME WAGE OF THE LOW PRODUCTIVITY WORKER BUT HAS TO PRODUCE A LARGER OUTPUT. HE IS THEREFORE BETTER OFF BY SIGNING THE CONTRACT OFFERED TO THE LOW PRODUCTIVITY WORKER BECAUSE BY SO DOING HE GETS THE SAME WAGE, BUT CAN PRODUCE THE REQUIRED OUTPUT IN A FRACTION OF ONE HOUR (HE IS MORE PRODUCTIVE) AND CAN REST FOR THE REMAINING TIME

TO AVOID THIS PROBLEM, THE HIGH-PRODUCTIVITY WORKERS MAY TRY TO SIGNAL THEIR TYPE H THROUH THE COSTLY SIGNAL OF EDUCATION

education as signal :

② education is costly  
and more costly for  
low quality agents

WORKER'S UTILITY

$$U(e, w) = w - e c \quad \begin{matrix} c_H \\ c_L \end{matrix}$$

$e$  = education       $c$  effort cost of education  
 $c_L > c_H$

W



slope  $C_L$

$$U = W - C_L \cdot e$$
$$\frac{\partial U / \partial e}{\partial U / \partial W} = -C_L$$

INDIFFERENCE CURVES OF  
TYPE L WORKER

$$MRS = - \frac{MU_e}{MU_w}$$

$$MRS = +C$$

W



$e_L$

INDIFFERENCE CURVES OF  
TYPE H WORKER

slope  $C_H$

$$C_L > C_H$$

$e_H$

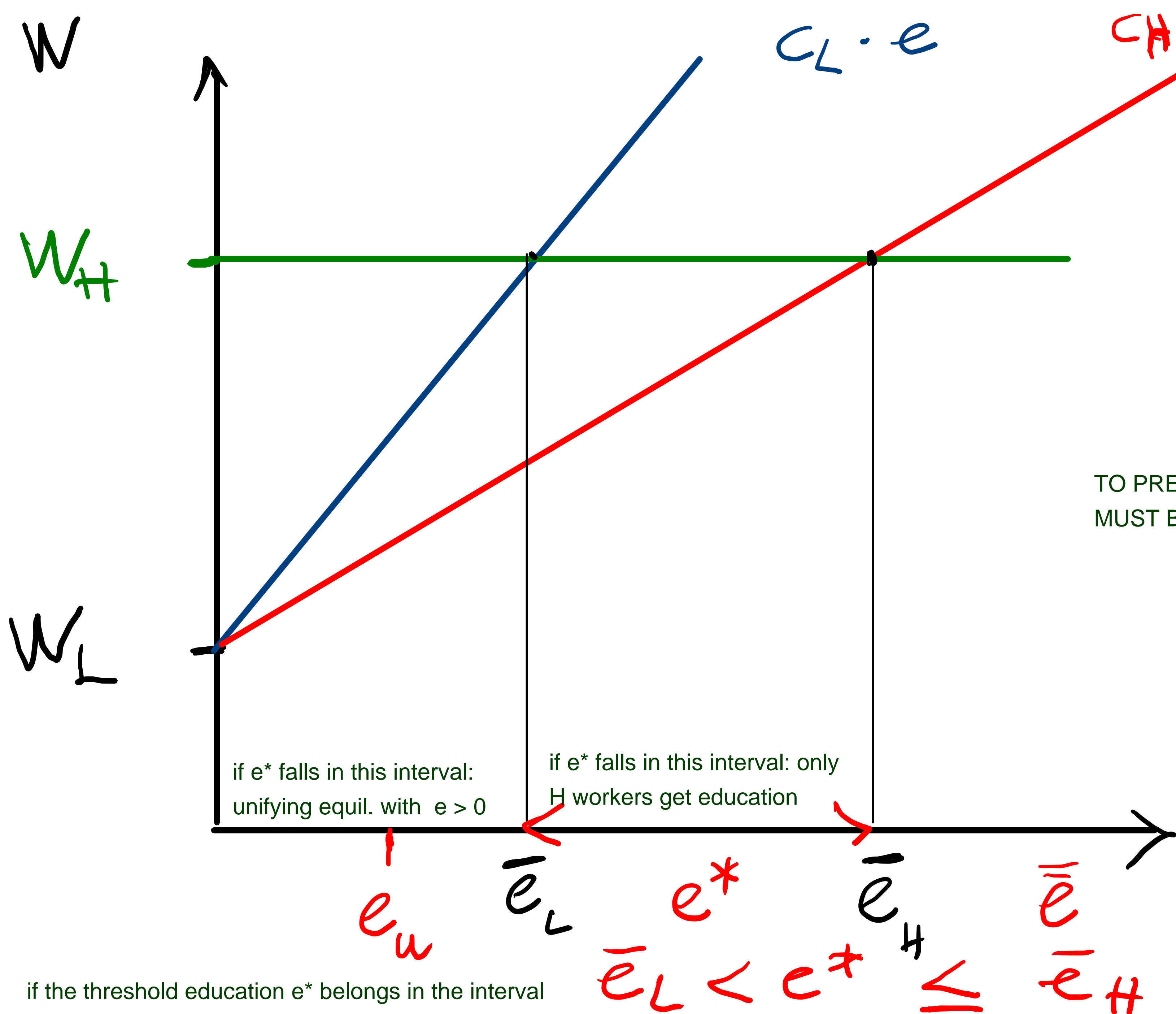
(2)

firms offer wage  $W^H$   
to workers with education  $e^*$   
(OR HIGHER).

if  $e < e^*$  THEN  $W = W^L < W^H$

IN THIS WAY, FIRMS ARE TRYING TO CONVINCE THE H WORKERS TO USE THEIR FULL PRODUCTIVE POTENTIAL

under what conditions  
will  $e^*$  separate the  
market?



$$u = W - C_L \cdot e$$

$$u = \text{constant}$$

$$W - C_L \cdot e = u$$

$$C_L \cdot e = W - u$$

$$W = C_L \cdot e + u$$

TO PRESERVE WELFARE UNCHANGED, HIGHER EDUCATION  
MUST BE COMPENSATED BY HIGHER WAGE EARNING

$\bar{e}_L$  max education  
for L

$\bar{e}_H$  max educat.  
for H

$e$

$e^*$

if the threshold education  $e^*$  belongs in the interval  $\bar{e}_L < e^* \leq \bar{e}_H$  then we have separating equilibria through signalling



Separating equilibrium  
through signalling if  
and only if:

$$\bar{e}_L < e^* \leq \bar{e}_H$$